## PHA5127

Case Study \#4
Fall 2005

1. Jonathan Weasley is put on aminoglycoside therapy and given an i.v. bolus injection of 10 mg of drug A, which has a clearance rate equal to the creatinine clearance and a volume of distribution of 26 L . This 34 year old man had a serum creatinine level of 0.6 $\mathrm{mg} / \mathrm{dL}$. Jonathan is $5^{\prime} 9^{\prime \prime}$ and weighs 220 lbs .
a. What is his creatinine clearance?
b. What is the $\mathrm{k}_{\mathrm{e}}$ ?
c. What is the half-life, $\mathrm{t}_{1 / 2}$ ?
d. What is the $\mathrm{C}_{\max }$ ?
e. What is the $\mathrm{AUC}_{\infty}$ ?

Height $_{\text {inches }}=5 \mathrm{ft} *$ 12inches + 9inches $=69$ inches
$I B W_{\text {male }}=50 \mathrm{~kg}+2.3 \mathrm{~kg} \times\left(\right.$ Height $_{\text {inches }}-60$ inches $)=50 \mathrm{~kg}+2.3 \mathrm{~kg} \times(69-60)$ inches
$I B W_{\text {male }}=70.7 \mathrm{~kg}$
Weight $(\mathrm{kg})=220 \mathrm{lbs}\left(\frac{1 \mathrm{~kg}}{2.2 \mathrm{lbs}}\right)=100 \mathrm{~kg}$
$\frac{T B W}{I B W}=\frac{100 \mathrm{~kg}}{70.7 \mathrm{~kg}} * 100 \%=141 \%$.
Exceeds 20\%. So Jonathan would be considered obese. Use ABW to calculate CrCL.
$A B W=I B W+0.4 \times(T B W-I B W)=70.7 \mathrm{~kg}+0.4 \times(100 \mathrm{~kg}-70.7 \mathrm{~kg})=82.4 \mathrm{~kg}$
$C r C L_{\text {male }}=\frac{(140-\text { age }) \times A B W}{72 \times \text { Serum Clearance }}=\frac{(140-34) \times 82.4 \mathrm{~kg}}{72 \times 0.6^{m g} / \mathrm{dL}}=202.2 \mathrm{~mL} / \mathrm{min}$
a) $C r C L_{\text {male }}=202.2 \mathrm{~mL} / \mathrm{min}\left(\frac{1 \mathrm{~L}}{1000 \mathrm{~mL}}\right)\left(\frac{60 \mathrm{~min}}{1 \mathrm{hr}}\right)=12.1 \mathrm{~L} / \mathrm{hr}$
$C L=C r C L=k_{e} \times V_{d}$
b) $k_{e}=\frac{C L}{V_{d}}=\frac{202.2 \mathrm{~mL} / \mathrm{min}}{26 L}\left(\frac{1 L}{1000 \mathrm{~mL}}\right)=0.0078 \mathrm{~min}^{-1}=0.47 \mathrm{hr}^{-1}$

Please note that this question poses a special situation in which it was assumed that the $\mathrm{CL}=\mathrm{CrCL}$ (as stated above). This is not always true. If it wasn't for this assumption, you would use the eqn $\mathrm{k}_{\mathrm{e}}=0.00293(\mathrm{CrCL})+0.014$ to calculate $\mathrm{k}_{\mathrm{e}}$.
c) $t_{1 / 2}=\frac{\ln (2)}{k_{e}}=\frac{\ln (2)}{0.0078 \mathrm{~min}^{-1}}=89 \mathrm{~min} s=1.5 \mathrm{hrs}$
d) $C_{\text {max }}=C_{o}=\frac{\text { Dose }}{V_{d}}=\frac{10 \mathrm{mg}}{26 \mathrm{~L}}=0.38 \mathrm{mg} / \mathrm{L}$
e) $A U C_{\infty}=\frac{\text { Dose }}{C L}=\frac{10 \mathrm{mg}}{202.2 \mathrm{~mL} / \mathrm{min}}=0.049(\mathrm{mg} \cdot \mathrm{min} / \mathrm{mL})=0.824(\mathrm{mg} \cdot \mathrm{hr} / \mathrm{L})$
2. Six other patients are also put on similar therapy and given the same treatment (an i.v. bolus injection of 10 mg of drug A). Please consider the following cases and answer their corresponding questions (Hint. Use the PK simulations for one compartment i.v. bolus models. Also note, that Jonathan had a fu of 0.1, fu $u_{T}$ of 0.17, and $C L_{i}$ of $140 \mathrm{~L} / \mathrm{h}$ ):

Patient 1: Has the same $\mathrm{V}_{\mathrm{d}}$ as Jonathan but has double the clearance rate. Has the following parameters increased, decreased, or stayed the same: i) $C_{m a x}$, ii) $k_{e}$, iii) $t_{1 / 2}$, and iv) $\mathrm{AUC}_{\infty}$ ?

Patient 2: Has the same clearance rate as Jonathan but twice the $\mathrm{V}_{\mathrm{d}}$. Has the following parameters increased, decreased, or stayed the same: i) $C_{\max }$, ii) $\mathrm{k}_{\mathrm{e}}$, iii) $\mathrm{t}_{1 / 2}$, and iv) $\mathrm{AUC}_{\infty}$ ?

Patient 3: Has the half the clearance rate and $\mathrm{V}_{\mathrm{d}}$ as Jonathan. Has the following parameters increased, decreased, or stayed the same: i) $C_{m a x}$, ii) $k_{e}$, iii) $t_{1 / 2}$, and iv) $\mathrm{AUC}_{\infty}$ ?

Patient 4: Is given drug B instead which has half the fraction of drug bound in plasma (in comparison to drug A) but the fraction of drug bound in tissue and the intrinsic clearance is the same. Has the following parameters increased, decreased, or stayed the same: i) $C_{\text {max }}$, ii) $k_{e}$, iii) $V_{d}$, iv) CL, v) $t_{1 / 2}$, vi) $E$, vii) $F$, and viii) $A U C_{\infty}$ ? Drug B is eliminated by liver only.

Patient 5: Is given drug C instead which has twice the intrinsic clearance as drug A (The fraction bound in plasma and tissue is the same as Jonathan's). Has the following parameters increased, decreased, or stayed the same: i) $C_{m a x}$, ii) $k_{e}$, iii) $V_{d}$, iv) $\left.C L, ~ v\right) t_{1 / 2}$, vi) E , vii) F , and viii) $\mathrm{AUC}_{\infty}$ ? Drug C is eliminated by the liver only.

Patient 6: Is given drug D instead. The drug is eliminated by the kidney only (Note: no tubular reabsorption or secretion occurs). If the fraction of drug unbound in tissue is actually twice than expected, does the following parameters increase, decrease, or stay the same: i) $C_{m a x}$, ii) $k_{e}$, iii) $V_{d}$, iv) $\left.C L, ~ v\right) t_{1 / 2}$, and vi) $A U C_{\infty}$ ? Note: the patient has a fu and initial $\mathrm{fu}_{\mathrm{T}}$ of 0.1 and the clearance is equal to the maximum possible for this drug.

Please Note: For questions 1-3, use the excel IV bolus single dose simulation. For questions $4 \& 5$, use the excel IV bolus physiological model (hepatic). For question 6, use the excel IV bolus physiological model (GFR). All patients are given a low extraction drug.

## Patient 1

$$
\begin{array}{ll}
C_{\max }=C_{o}=\frac{\text { Dose }}{V_{d}} & \text { Nothing changes, so } C_{\max } \text { stays the same. } \\
k_{e}=\frac{C L}{V_{d}} & \Rightarrow \frac{2 C L}{V_{d}}=2 k_{e} \quad \text { So } k_{e} \text { doubles. }
\end{array}
$$

$$
\begin{array}{ll}
t_{1 / 2}=\frac{\ln (2)}{k_{e}} & \Rightarrow \frac{\ln (2)}{2 k_{e}}=0.5 \cdot t_{1 / 2} \quad \text { So } t_{1 / 2} \text { is halved. } \\
A U C_{\infty}=\frac{C_{\max }}{k_{e}} & \Rightarrow \frac{C_{\max }}{2 k_{e}}=0.5 \cdot A U C_{\infty} \quad \text { So } A U C_{\infty} \text { is halved. }
\end{array}
$$

Patient 2

$$
\begin{array}{ll}
C_{\max }=C_{o}=\frac{\text { Dose }}{V_{d}} & \Rightarrow \frac{\text { Dose }}{2 V_{d}}=0.5 \cdot C_{\max } \quad \text { So } C_{\max } \text { is halved. } \\
k_{e}=\frac{C L}{V_{d}} & \Rightarrow \frac{C L}{2 V_{d}}=0.5 \cdot k_{e} \quad \text { So } k_{e} \text { is halved. } \\
t_{1 / 2}=\frac{\ln (2)}{k_{e}} & \Rightarrow \frac{\ln (2)}{0.5 k_{e}}=2 \cdot t_{1 / 2} \quad \text { So } t_{1 / 2} \text { is doubled. } \\
A U C_{\infty}=\frac{C_{\max }}{k_{e}} & \Rightarrow \frac{0.5 C_{\max }}{0.5 k_{e}}=A U C_{\infty} \quad \text { So } A U C_{\infty} \text { stays the same. }
\end{array}
$$

## Patient 3

$$
\begin{array}{ll}
C_{\max }=C_{o}=\frac{\text { Dose }}{V_{d}} & \Rightarrow \frac{\text { Dose }}{0.5 V_{d}}=2 C_{\max } \quad \text { So } C_{\max } \text { is doubled. } \\
k_{e}=\frac{C L}{V_{d}} & \Rightarrow \frac{0.5 C L}{0.5 V_{d}}=k_{e} \quad \text { So } k_{e} \text { stays the same. } \\
t_{1 / 2}=\frac{\ln (2)}{k_{e}} & \Rightarrow \frac{\ln (2)}{k_{e}}=t_{1 / 2} \quad \text { So } t_{1 / 2} \text { stays the same. } \\
A U C_{\infty}=\frac{C_{\max }}{k_{e}} & \Rightarrow \frac{2 C_{\max }}{k_{e}}=2 \cdot A U C_{\infty} \quad \text { So } A U C_{\infty} \text { is doubled. }
\end{array}
$$

## Patient 4

$$
f b=1-f u=1-0.1=0.9
$$

$$
0.5 f b=0.45
$$

$$
f u^{\prime}=1-0.45=0.55
$$

$$
\begin{array}{ll}
V_{d}=V_{P}+V_{T} \cdot \frac{f u}{f u_{T}} & \Rightarrow \uparrow V_{d} \\
C_{\max }=C_{o}=\frac{D o s e}{V_{d}} & \Rightarrow \downarrow C_{\max } \\
C L=C L_{H}=\frac{Q \times C L_{i} \times f u}{Q+C L_{i} \times f u} & \Rightarrow \uparrow C L \\
k_{e}=\frac{C L}{V_{d}} & \Rightarrow \downarrow k_{e} \\
t_{1 / 2}=\frac{\ln (2)}{k_{e}} & \Rightarrow \uparrow t_{1 / 2}
\end{array}
$$

$$
\begin{array}{ll}
A U C_{\infty}=\frac{C_{\mathrm{max}}}{k_{e}} & \Rightarrow \downarrow A U C_{\infty} \\
E_{H}=\frac{C L_{i} \times f u}{Q+C L_{i} \times f u} & \Rightarrow \uparrow E_{H} \\
F(\%)=(1-E) \times 100 \% & \Rightarrow \downarrow F
\end{array}
$$

Patient 5

$$
\begin{aligned}
& \leftrightarrow C_{\max } \\
& \uparrow k_{e} \\
& \leftrightarrow V_{d} \\
& \uparrow C L \\
& \downarrow t_{1 / 2} \\
& \uparrow E_{H} \\
& \downarrow F \\
& \downarrow A U C_{\infty}
\end{aligned}
$$

Patient 6
$\uparrow C_{\text {max }}$
$\uparrow k_{e}$
$\downarrow V_{d}$
$\leftrightarrow C L$
$\downarrow t_{1 / 2}$
$\leftrightarrow A U C_{\infty}$

